



OSWEGO CITY ENGINEER
WILLIAM J. BARLOW, JR. MAYOR

PROJECT: OSWEGO CASTINGS #738033

SHEET: 1 OF 7 SUBJECT: CONC. SLAB ANALYSIS

CALCULATED BY: JH

DATE: 1/29/2020

CHECKED BY: _____

DATE: _____

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DETERMINE THE LOADING FROM A FULL TANK:

$$V_{TANK} = 10,000 \text{ GAL} = 1337 \text{ FT}^3$$

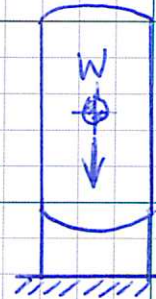
SPECIFIC GRAVITY OF LIQUID @ 60°F = 1.01

DENSITY OF WATER @ 60°F = 62.366 LB/FT³

$$W = (1.01)(62.366 \text{ LB/FT}^3)(1337 \text{ FT}^3)$$

$$W = 84,217 \text{ LB}$$

∴ EACH POST WILL RECEIVE 21,054 LB.



ANALYSIS OF THE SLAB

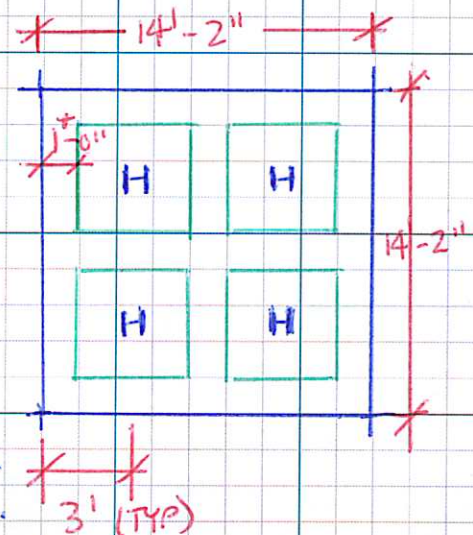
A_{SLAB} ≈ 200 SF

FOR ANALYSIS PURPOSES, SHEAR WILL BE CHECKED FOR A SINGLE POST.

THE ANALYSIS WILL INCLUDE BOTH ONE-WAY AND PUNCHING SHEAR, IN ACCORDANCE WITH ACI 318.

DUE TO THE LARGE PLATES, THE LIKELIHOOD OF A SHEAR FAILURE IS MINIMAL.

FOR ARGUMENTS SAKE, IT WILL BE ASSUMED AN AREA 16" x 16" WILL INFLUENCE THE SHEAR ZONE. THIS MATCHES THE SHIM MATERIAL DIMENSIONS.





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SHEET: 2 OF 7 SUBJECT: _____

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ANALYSIS OF A SINGLE POST

BASED ON RECORDS OF THE BACKFILL USED UNDER THE CAP, THE IN-PLACE DENSITY RESULTS SHOW A DENSITY OF APPROX 125 LB/FT³.

THIS TYPICAL OF A WELL GRADED GRAVEL WITH GOOD COMPACTION.

NO SPECIFICATIONS WERE PROVIDED.

∴ AN ASSUMED BEARING PRESSURE IS 5000 PSF FOR A WELL GRADED GRAVEL.

$$q_{eff} = (5000 \text{ PSF} - 100 \text{ PSF}_{CONC}) = 4900 \text{ PSF} \quad \text{SAY } \underline{4500 \text{ PSF}}$$

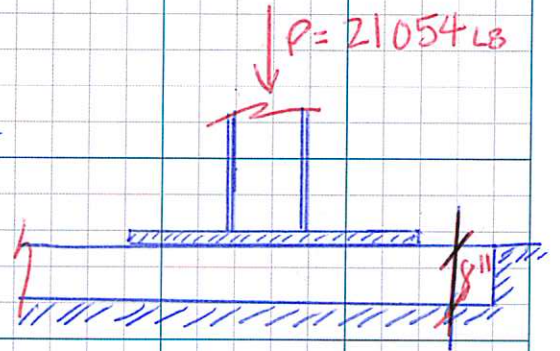
$$A_{REQ} = \frac{21054 \text{ LB}}{4500 \text{ LB/SF}} = 4.68 \text{ SQ FT.}$$

EACH POST HAS A MINIMUM OF A 48" x 48" x 1/2" PLATE OF STEEL.

FOR ANALYSIS PURPOSES, ASSUME A CONCRETE AREA OF 16 SQ FT.

$$\therefore p_u = \frac{1.6(21054 \text{ LB})}{16 \text{ FT}^2} = 2105 \text{ PSF}$$

$$\text{DEPTH TO REINFORCEMENT, } d = 8" - 3" \text{ COVER} = 5"$$





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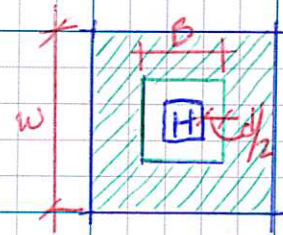
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CHECK PUNCHING SHEAR

$$B = \text{column} + d = 16" + 5" = 21"$$

$$V = p_u (w^2 - B^2) = 2105 \text{ PSF} (4 \text{ FT}^2 - 1.75 \text{ FT}^2)$$

$$V = 27.233 \text{ LB SHEAR FORCE}$$



CONCRETE SHEAR CAPACITY

$$a) \phi V_c = (0.85) \left(2 + \frac{4}{\beta_c} \right) \sqrt{f'_c} b_o d = (0.85) \left(2 + \frac{4}{1} \right) \sqrt{4000 \text{ PSI}} (84") (5")$$

$$= 135,472 \text{ LB}$$

$$b) \phi V_c = (0.85) \left(\frac{\alpha_s d}{b_o} + 2 \right) \sqrt{f'_c} b_o d = (0.85) \left(\frac{20(5")}{84"} + 2 \right) \sqrt{4000 \text{ PSI}} (84") (5")$$

$$\phi V_c = 72,037 \text{ LB}$$

$$c) \phi V_c = (0.85) 4 \sqrt{f'_c} b_o d = (0.85) (4) \sqrt{4000 \text{ PSI}} (84") (5")$$

$$\phi V_c = 90,315 \text{ LB}$$

USING THE SMALLEST VALUE FOR ϕV_c

$$72,037 \text{ LB} > 27,233 \text{ LB}$$

✓ OK



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SHEET: 4 OF 7 SUBJECT: _____

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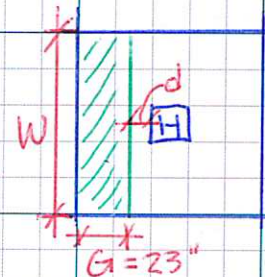
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CHECK ONE-WAY SHEAR

$$V_u = p_u W G = (2105 \text{ PSF})(4 \text{ FT})(1.92 \text{ FT})$$

$$V_u = 16166 \text{ LB}$$

$$\begin{aligned} \phi V_c &= (0.85)(2) \sqrt{f_c'} b_w d \\ &= (0.85)(2) \sqrt{4000 \text{ PSI}} (48 \text{ IN})(5 \text{ IN}) \\ &= 25804 \text{ LB} \end{aligned}$$



$$25804 \text{ LB} > 16166 \text{ LB} \quad \checkmark \text{ OK}$$

CHECK BENDING MOMENT

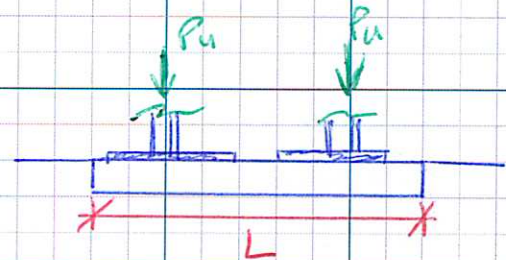
DUE TO THE SLAB ACTING AS A MAT FOUNDATION, A MOMENT ANALYSIS WILL BE DONE LOOKING AT 2 POTS ACTING ON HALF OF THE SLAB.

$$L = 14.11666 \text{ FT}$$

$$W = L/2 = 7.0833 \text{ FT}$$

$$A_{\text{REQ}} = \frac{42108 \text{ LB}}{4500 \text{ PSF}} = 9.36 \text{ SQ FT.}$$

$$A_{\text{PROV}} = W \times L = 100.35 \text{ SQ FT.}$$



$$p_u = \frac{1.6 (42108 \text{ LB})}{100.35 \text{ SQ FT}} = 671 \text{ PSF ON THE FLOOR}$$



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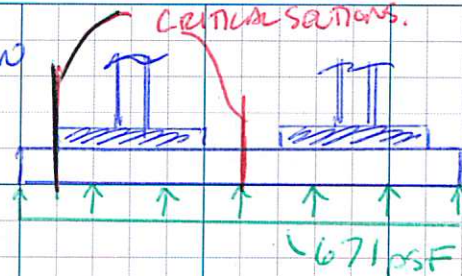
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USING THE ATTACHED CALCULATION

$$M_{u1} = 21,389 \text{ FT-LB NEAR POST}$$

$$M_{u2} = 18,236 \text{ FT-LB MID SPAN}$$



CHECK THE DESIGN STEEL

$$A_{s\text{PROV}} = 6 \times 6 \times 10/10 \text{ WWF} = (0.028 \text{ in}^2/\text{FT})(7.0833) = \underline{0.198 \text{ in}^2}$$

AS REQ M_{u2}

$$R_{eq} \bar{K} = \frac{M_u}{\phi b d^2} = \frac{(18,236 \text{ FT-LB})(12 \text{ IN/FT})}{(0.9)(7.0833)(12)(5 \text{ IN})^2} = 0.1144 \text{ KSI}$$

$$\rho = 0.0070$$

$$\therefore A_{s\text{REQ}} = \rho b d = (0.0070)(7.0833)(12)(5) = 0.85 \text{ in}^2$$

NOT ENOUGH STEEL IS PROVIDED. THIS IS EVIDENCED BY A MOMENT CRACK DISCOVERED IN THE SLAB (PIC A)

$\therefore$ TO PREVENT FURTHER DAMAGE, THE AMOUNT OF LIQUID SHOULD BE LIMITED.



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ONLY 23.3 % OF THE REQUIRED STEEL IS PROVIDED.

$$\rho = \frac{A_s}{bd} = 0.0005$$

NOMINAL CAPACITY OF SLAB

$$\phi M_n = \frac{\phi b d^2}{12} \bar{k}$$

$$\bar{k} = f'_c \omega (1 - 0.59 \omega)$$

$$\omega = \rho \frac{F_y}{F'_c} = (0.0005) \frac{60,000 \text{ PSI}}{4,000 \text{ PSI}} = 0.0075$$

$$\bar{k} = (4 \text{ ksi}) (0.0075) (1 - 0.59 (0.0075)) = 0.0299 \text{ ksi}$$

$$\phi M_n = \frac{(0.9)(85 \text{ in})(5 \text{ in})^2}{12} (0.0299 \text{ ksi}) = 4.765 \text{ FT-KIP}$$

4765 FT-LB.

Approx 1225 LB/FT IS THE NOMINAL LOADING. THIS
EQUATES TO A UNIFORM SOIL LOAD OF 173 PSF.

$$P_{\text{Nom}} = \frac{A_{\text{Area}} P_u}{1.6} = \frac{(100.35 \text{ SQ FT})(173 \text{ PSF})}{1.6}$$

$$P_{\text{Nom}} = 10,850 \text{ LB PER LEG.}$$



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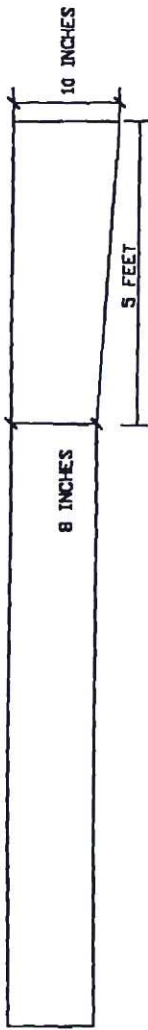
WITH 10 850 LB PER POST, A TOTAL LOAD IS

$$W_{\text{Nom}} = 43,400 \text{ LB.}$$

THIS IS APPROX 51.5% OF THE TANK CAPACITY.

∴ THE TANK SHOULD ONLY BE FILLED W/ 5000 gal
TO PREVENT CREEP PROPAGATION.



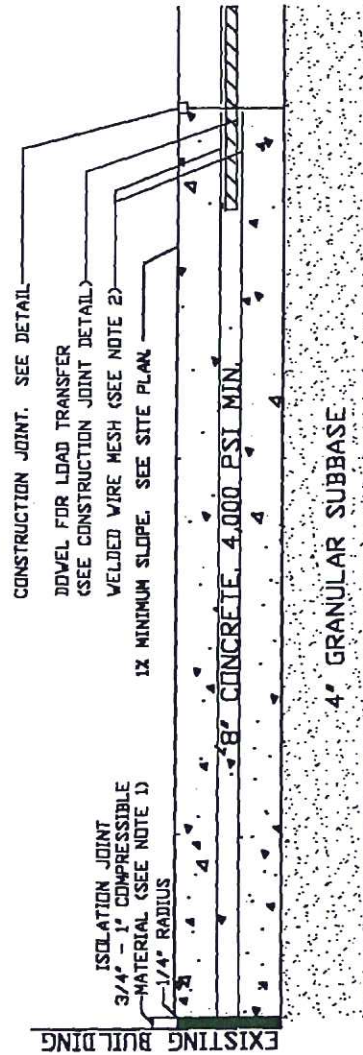


CONCRETE PAD - EDGE THICKENING

NTS

NOTES:

1. SLAB TO BE THICKENED AT ALL EXTERNAL EDGES WHICH ARE LOADED, INCLUDING DOORWAYS
2. SLAB TO BE THICKENED TO 10", AND TAPERED BACK TO 8" OVER A 5' DISTANCE.

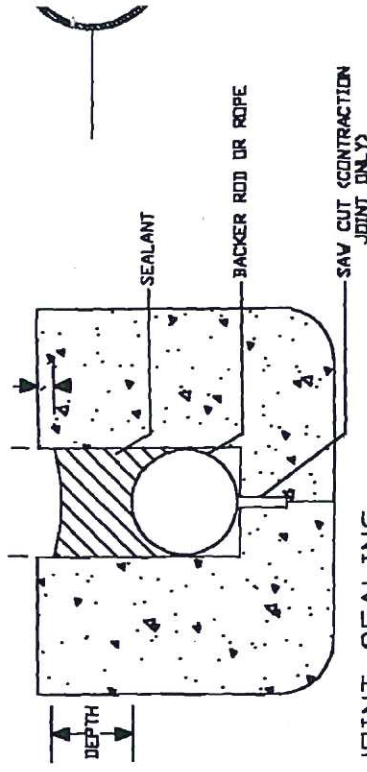


CONCRETE PAD - CROSS SECTION

NTS

NOTES:

1. INSTALL 1" NONEXTRUDABLE, PREFORMED COMPRESSIBLE MATERIAL BETWEEN SLAB AND ANY EXISTING BUILDINGS.
2. REINFORCING MESH: 2 LAYERS OF 10 GAUGE WIRE AT 6" CENTERS. WIRE TO BE 60,000 PSI YIELD STRENGTH WELDED WIRE MESH. INSTALL MESH AT 3" FROM TOP AND 3" FROM BOTTOM OF CONCRETE. MESH SHALL NOT EXTEND THROUGH THE CONTRACTION JOINT.

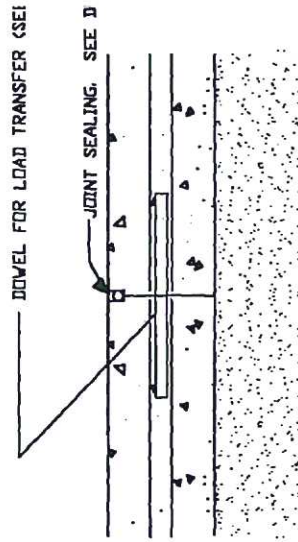


JOINT SEALING

NTS

NOTES:

1. SEALANT TO BE SIKAFLEX -2C, SL OR APPROVED EQUAL
2. MINIMUM DEPTH 1/4", MAXIMUM DEPTH 1/2"
3. $\frac{\text{DEPTH}}{\text{WIDTH}} = \text{SHAPE FACTOR} \approx 0.5$



CONSTRUCTION JOINT

NTS

NOTES:

1. INTERNAL JOINTS (CONSTRUCTION OR CONTRACTION) TO BE SPACED NO GREATER THAN 15' O.C.
2. PROVIDE DOVELS AT ALL INTERNAL JOINTS. INSTALL DOVEL AT MID-DEPTH OF JOINT WITH A 50 KSI MINIMUM YIELD STRENGTH DOVEL DIMENSIONS: DIAMETER 1", TOTAL LENGTH 18". SPACING: DOVELS SHALL MEET THE REQUIREMENTS OF AASHTO M254 FOR LOAD DELIVERY, PULLOUT, CORROSION, AND ABRASION.
3. END DOVELS SHALL BE 6" FROM THE EDGE OF PAVEMENT. INTERVENING DOVELS SHALL BE SPACED 12" +/- 1/2" APART. DOVEL CENTERLINES SHALL BE AT MID-DEPTH OF CONCRETE +/- 1/4". DOVELS SHALL BE PARALLEL TO THE CENTERLINE TO WITHIN 1/8" PER FOOT. THE DOVELS SHALL BE CENTERED ON THE JOINT.
5. REINFORCEMENT DOES NOT EXTEND THROUGH CONTRACTION JOINT

A



B



C



D





TABLE A-10 Coefficient of Resistance ($\bar{k}$) Versus Reinforcement Ratio (ρ)
 ($f'_c = 4000$ psi; $f_y = 60,000$ psi; Units of $\bar{k}$ Are ksi)

ρ	$\bar{k}$	ρ	$\bar{k}$	ρ	$\bar{k}$	ρ	$\bar{k}$
0.0010	0.0595	0.0036	0.2091	0.0062	0.3516	0.0088	0.4870
0.0011	0.0654	0.0037	0.2148	0.0063	0.3570	0.0089	0.4921
0.0012	0.0712	0.0038	0.2204	0.0064	0.3623	0.0090	0.4971
0.0013	0.0771	0.0039	0.2259	0.0065	0.3676	0.0091	0.5022
0.0014	0.0830	0.0040	0.2315	0.0066	0.3729	0.0092	0.5072
0.0015	0.0889	0.0041	0.2371	0.0067	0.3782	0.0093	0.5122
0.0016	0.0946	0.0042	0.2427	0.0068	0.3835	0.0094	0.5172
0.0017	0.1005	0.0043	0.2482	0.0069	0.3888	0.0095	0.5222
0.0018	0.1063	0.0044	0.2538	0.0070	0.3941	0.0096	0.5272
0.0019	0.1121	0.0045	0.2593	0.0071	0.3993	0.0097	0.5322
0.0020	0.1179	0.0046	0.2648	0.0072	0.4046	0.0098	0.5372
0.0021	0.1237	0.0047	0.2703	0.0073	0.4098	0.0099	0.5421
0.0022	0.1294	0.0048	0.2758	0.0074	0.4150	0.0100	0.5471
0.0023	0.1352	0.0049	0.2813	0.0075	0.4202	0.0101	0.5520
0.0024	0.1410	0.0050	0.2868	0.0076	0.4254	0.0102	0.5569
0.0025	0.1467	0.0051	0.2922	0.0077	0.4306	0.0103	0.5618
0.0026	0.1524	0.0052	0.2977	0.0078	0.4358	0.0104	0.5667
0.0027	0.1581	0.0053	0.3031	0.0079	0.4410	0.0105	0.5716
0.0028	0.1638	0.0054	0.3086	0.0080	0.4461	0.0106	0.5765
0.0029	0.1695	0.0055	0.3140	0.0081	0.4513	0.0107	0.5814
0.0030	0.1752	0.0056	0.3194	0.0082	0.4564	0.0108	0.5862
0.0031	0.1809	0.0057	0.3248	0.0083	0.4615	0.0109	0.5911
0.0032	0.1866	0.0058	0.3302	0.0084	0.4666	0.0110	0.5959
0.0033	0.1922	0.0059	0.3356	0.0085	0.4718	0.0111	0.6008
0.0034	0.1979	0.0060	0.3409	0.0086	0.4768	0.0112	0.6056
0.0035	0.2035	0.0061	0.3463	0.0087	0.4819	0.0113	0.6104

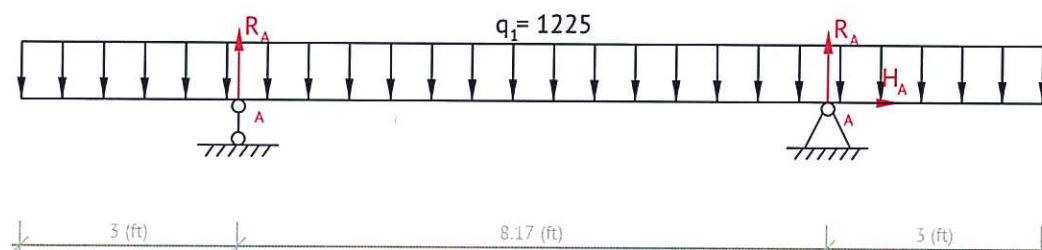
TABLE A-10 (CONT.) Coefficient of Resistance ($\bar{k}$) Versus Reinforcement Ratio (ρ)
 ($f'_c = 4000$ psi; $f_y = 60,000$ psi; Units of $\bar{k}$ Are ksi)

ρ	$\bar{k}$	ρ	$\bar{k}$	ρ	$\bar{k}$	ρ	$\bar{k}$
0.0114	0.6152	0.0140	0.7362	0.0165	0.8459	0.0190	0.9489
0.0115	0.6200	0.0141	0.7407	0.0166	0.8501	0.0191	0.9529
0.0116	0.6248	0.0142	0.7452	0.0167	0.8544	0.0192	0.9568
0.0117	0.6295	0.0143	0.7497	0.0168	0.8586	0.0193	0.9608
0.0118	0.6343	0.0144	0.7542	0.0169	0.8628	0.0194	0.9648
0.0119	0.6390	0.0145	0.7587	0.0170	0.8670	0.0195	0.9687
0.0120	0.6438	0.0146	0.7632	0.0171	0.8712	0.0196	0.9726
0.0121	0.6485	0.0147	0.7675	0.0172	0.8754	0.0197	0.9765
0.0122	0.6532	0.0148	0.7720	0.0173	0.8796	0.0198	0.9804
0.0123	0.6579	0.0149	0.7765	0.0174	0.8837	0.0199	0.9843
0.0124	0.6626	0.0150	0.7809	0.0175	0.8879	0.0200	0.9882
0.0125	0.6673	0.0151	0.7853	0.0176	0.8920	0.0201	0.9921
0.0126	0.6720	0.0152	0.7897	0.0177	0.8961	0.0202	0.9960
0.0127	0.6766	0.0153	0.7941	0.0178	0.9003	0.0203	0.9998
0.0128	0.6813	0.0154	0.7984	0.0179	0.9044	0.0204	1.0037
0.0129	0.6859	0.0155	0.8028	0.0180	0.9085	0.0205	1.0075
0.0130	0.6905	0.0156	0.8072	0.0181	0.9116	0.0206	1.0113
0.0131	0.6951	0.0157	0.8115	0.0182	0.9166	0.0207	1.0152
0.0132	0.6998	0.0158	0.8158	0.0183	0.9207	0.0208	1.0190
0.0133	0.7044	0.0159	0.8202	0.0184	0.9248	0.0209	1.0227
0.0134	0.7089	0.0160	0.8245	0.0185	0.9288	0.0210	1.0265
0.0135	0.7135	0.0161	0.8288	0.0186	0.9328	0.0211	1.0303
0.0136	0.7181	0.0162	0.8331	0.0187	0.9369	0.0212	1.0341
0.0137	0.7226	0.0163	0.8373	0.0188	0.9409	0.0213	1.0378
0.0138	0.7272	0.0164	0.8416	0.0189	0.9449	0.0214	1.0416
0.0139	0.7317						

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Clear beam

Save link on this calculation

**Select units**

Units of measurement:

Foot (ft)

Units of force:

Pound-force (lbf)

Setting the length of beamLength of beam L , (ft):

14.1666

Setting the support of beam

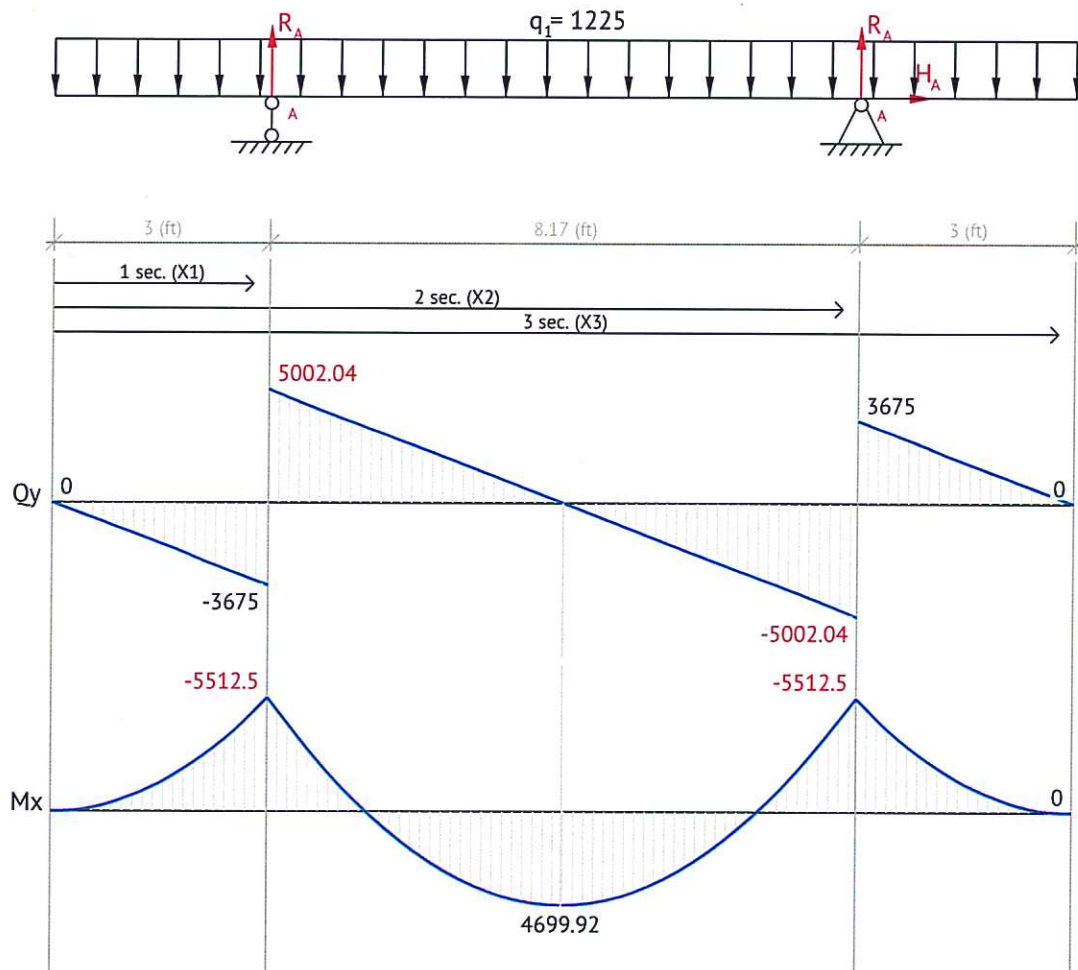
at the point B

at the point A

Setting the loads of beam $q_1 = -1225$ (lbf/ft)**Setting the bending diagrams of beam**

- ☒ Calculate the reactions at the supports of a beam
- ☒ Bending moment diagram (BMD) ☒ Shear force diagram (SFD) ☐ Axial force diagram
- ☒ Invert Diagram of Moment (BMD) - Moment is positive, when tension at the bottom of the beam

SOLVE



Calculate the reactions at the supports of a beam

1. A beam is in equilibrium when it is stationary relative to an inertial reference frame. The following conditions are satisfied when a beam, acted upon by a system of forces and moments, is in equilibrium.

$$\Sigma F_x = 0: \quad H_B = 0$$

$\Sigma M_A = 0$: The sum of the moments about the roller support at the point A:

$$- q_1 * 14.1666 * (-3 + 14.1666/2) + R_B * 8.1666 = 0$$

$\Sigma M_B = 0$: The sum of the moments about the pin support at the point B:

$$q_1 * 14.1666 * (11.1666 - 14.1666/2) - R_A * 8.1666 = 0$$

2. Calculate reaction of pin support at the point B:

$$R_B = (q_1 * 14.1666 * (-3 + 14.1666/2)) / 8.1666 = (1225 * 14.1666 * (-3 + 14.1666/2)) / 8.1666 = 8677.04 \text{ (lbf)}$$

3. Calculate reaction of roller support at the point A:

$$R_A = (q_1 * 14.1666 * (11.1666 - 14.1666/2)) / 8.1666 = (1225 * 14.1666 * (11.1666 - 14.1666/2)) / 8.1666 = 8677.04 \text{ (lbf)}$$

4. Solve this system of equations:

$$H_B = 0 \text{ (lbf)}$$

5. The sum of the forces about the Oy axis is zero:

$$\Sigma F_y = 0: \quad - q_1 * 14.1666 + R_A + R_B = - 1225 * 14.1666 + 8677.04 * 1 + 8677.04 * 1 = 0$$

Draw diagrams for the beam

Consider first span of the beam $0 \leq x_1 < 3$

Determine the equations for the shear force (Q):

$$Q(x_1) = - q_1 * (x_1 - 0)$$

The values of Q at the edges of the span:

$$Q_1(0) = - 1225 * (0 - 0) = 0 \text{ (lbf)}$$

$$Q_1(3) = - 1225 * (3 - 0) = -3675 \text{ (lbf)}$$

Determine the equations for the bending moment (M):

$$M(x_1) = - q_1 * (x_1)^2 / 2$$

The values of M at the edges of the span:

$$M_1(0) = - 1225 * (0 - 0)^2 / 2 = 0 \text{ (lbf*ft)}$$

$$M_1(3) = - 1225 * (3 - 0)^2 / 2 = -5512.50 \text{ (lbf*ft)}$$

Consider second span of the beam $3 \leq x_2 < 11.1666$

Determine the equations for the shear force (Q):

$$Q(x_2) = -q_1(x_2 - 0) + R_A$$

The values of Q at the edges of the span:

$$Q_2(3) = -1225(3 - 0) + 8677.04 = 5002.04 \text{ (lbf)}$$

$$Q_2(11.17) = -1225(11.1666 - 0) + 8677.04 = -5002.04 \text{ (lbf)}$$

The value of Q on this span that crosses the horizontal axis. Intersection point:

$$x = 4.08$$

Determine the equations for the bending moment (M):

$$M(x_2) = -q_1(x_2)^2/2 + R_A(x_2 - 3)$$

The values of M at the edges of the span:

$$M_2(3) = -1225(3 - 0)^2/2 + 8677.04(3 - 3) = -5512.50 \text{ (lbf*ft)}$$

$$M_2(11.17) = -1225(11.17 - 0)^2/2 + 8677.04(11.17 - 3) = -5512.50 \text{ (lbf*ft)}$$

Local extremum at the point $x = 4.08$:

$$M_2(7.08) = -1225(7.08 - 0)^2/2 + 8677.04(7.08 - 3) = 4699.92 \text{ (lbf*ft)}$$

Consider third span of the beam $11.1666 \leq x_3 < 14.1666$ **Determine the equations for the shear force (Q):**

$$Q(x_3) = -q_1(x_3 - 0) + R_A + R_B$$

The values of Q at the edges of the span:

$$Q_3(11.17) = -1225(11.1666 - 0) + 8677.04 + 8677.04 = 3675 \text{ (lbf)}$$

$$Q_3(14.17) = -1225(14.1666 - 0) + 8677.04 + 8677.04 = 0 \text{ (lbf)}$$

Determine the equations for the bending moment (M):

$$M(x_3) = -q_1(x_3)^2/2 + R_A(x_3 - 3) + R_B(x_3 - 11.1666)$$

The values of M at the edges of the span:

$$M_3(11.17) = -1225(11.17 - 0)^2/2 + 8677.04(11.17 - 3) + 8677.04(11.17 - 11.1666) = -5512.50 \text{ (lbf*ft)}$$

$$M_3(14.17) = -1225(14.17 - 0)^2/2 + 8677.04(14.17 - 3) + 8677.04(14.17 - 11.1666) = 0 \text{ (lbf*ft)}$$

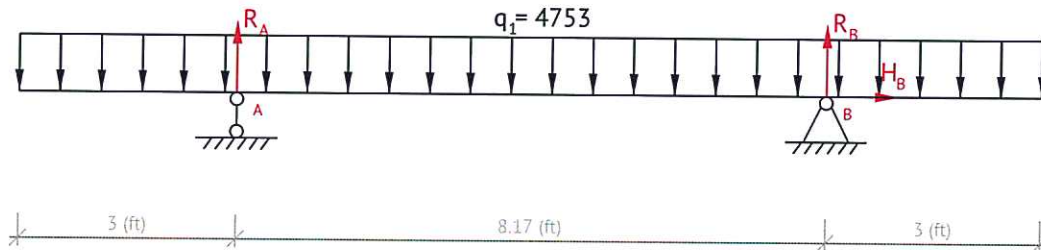
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Clear beam

Save link on this calculation

**Select units**

Units of measurement:

Foot (ft)

Units of force:

Pound-force (lbf)

Setting the length of beamLength of beam L , (ft):

14.1666

Setting the support of beam

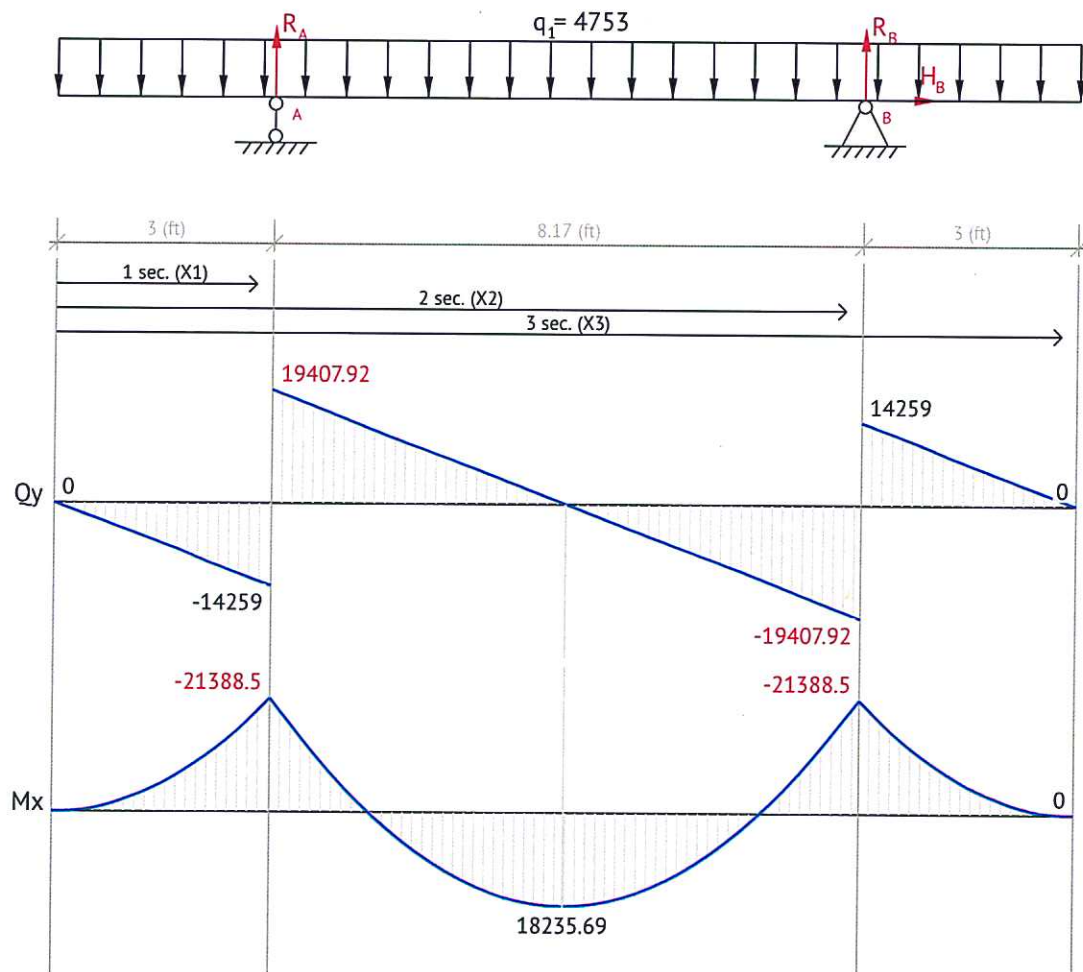
at the point B

at the point A

Setting the loads of beam $q_1 = -4753$ (lbf/ft)**Setting the bending diagrams of beam**

- ☒ Calculate the reactions at the supports of a beam
- ☒ Bending moment diagram (BMD) ☒ Shear force diagram (SFD) ☐ Axial force diagram
- ☒ Invert Diagram of Moment (BMD) - Moment is positive, when tension at the bottom of the beam

SOLVE



Calculate the reactions at the supports of a beam

1. A beam is in equilibrium when it is stationary relative to an inertial reference frame. The following conditions are satisfied when a beam, acted upon by a system of forces and moments, is in equilibrium.

$$\Sigma F_x = 0: \quad H_B = 0$$

$\Sigma M_A = 0$: The sum of the moments about the roller support at the point A:

$$- q_1 * 14.1666 * (-3 + 14.1666/2) + R_B * 8.1666 = 0$$

$\Sigma M_B = 0$: The sum of the moments about the pin support at the point B:

$$q_1 * 14.1666 * (11.1666 - 14.1666/2) - R_A * 8.1666 = 0$$

2. Calculate reaction of pin support at the point B:

$$R_B = (q_1 * 14.1666 * (-3 + 14.1666/2)) / 8.1666 = (4753 * 14.1666 * (-3 + 14.1666/2)) / 8.1666 = 33666.92 \text{ (lbf)}$$

3. Calculate reaction of roller support at the point A:

$$R_A = (q_1 * 14.1666 * (11.1666 - 14.1666/2)) / 8.1666 = (4753 * 14.1666 * (11.1666 - 14.1666/2)) / 8.1666 = 33666.92 \text{ (lbf)}$$

4. Solve this system of equations:

$$H_B = 0 \text{ (lbf)}$$

5. The sum of the forces about the Oy axis is zero:

$$\Sigma F_y = 0: \quad -q_1 * 14.1666 + R_A + R_B = -4753 * 14.1666 + 33666.92 * 1 + 33666.92 * 1 = 0$$

Draw diagrams for the beam

Consider first span of the beam $0 \leq x_1 < 3$

Determine the equations for the shear force (Q):

$$Q(x_1) = -q_1 * (x_1 - 0)$$

The values of Q at the edges of the span:

$$Q_1(0) = -4753 * (0 - 0) = 0 \text{ (lbf)}$$

$$Q_1(3) = -4753 * (3 - 0) = -14259 \text{ (lbf)}$$

Determine the equations for the bending moment (M):

$$M(x_1) = -q_1 * (x_1)^2 / 2$$

The values of M at the edges of the span:

$$M_1(0) = -4753 * (0 - 0)^2 / 2 = 0 \text{ (lbf*ft)}$$

$$M_1(3) = -4753 * (3 - 0)^2 / 2 = -21388.50 \text{ (lbf*ft)}$$

Consider second span of the beam $3 \leq x_2 < 11.1666$

Determine the equations for the shear force (Q):

$$Q(x_2) = -q_1 \cdot (x_2 - 0) + R_A$$

The values of Q at the edges of the span:

$$Q_2(3) = -4753 \cdot (3 - 0) + 33666.92 = 19407.92 \text{ (lbf)}$$

$$Q_2(11.17) = -4753 \cdot (11.1666 - 0) + 33666.92 = -19407.92 \text{ (lbf)}$$

The value of Q on this span that crosses the horizontal axis. Intersection point:

$$x = 4.08$$

Determine the equations for the bending moment (M):

$$M(x_2) = -q_1 \cdot (x_2)^2/2 + R_A \cdot (x_2 - 3)$$

The values of M at the edges of the span:

$$M_2(3) = -4753 \cdot (3 - 0)^2/2 + 33666.92 \cdot (3 - 3) = -21388.50 \text{ (lbf*ft)}$$

$$M_2(11.17) = -4753 \cdot (11.17 - 0)^2/2 + 33666.92 \cdot (11.17 - 3) = -21388.50 \text{ (lbf*ft)}$$

Local extremum at the point $x = 4.08$:

$$M_2(7.08) = -4753 \cdot (7.08 - 0)^2/2 + 33666.92 \cdot (7.08 - 3) = 18235.69 \text{ (lbf*ft)}$$

Consider third span of the beam $11.1666 \leq x_3 < 14.1666$ **Determine the equations for the shear force (Q):**

$$Q(x_3) = -q_1 \cdot (x_3 - 0) + R_A + R_B$$

The values of Q at the edges of the span:

$$Q_3(11.17) = -4753 \cdot (11.1666 - 0) + 33666.92 + 33666.92 = 14259 \text{ (lbf)}$$

$$Q_3(14.17) = -4753 \cdot (14.1666 - 0) + 33666.92 + 33666.92 = 0 \text{ (lbf)}$$

Determine the equations for the bending moment (M):

$$M(x_3) = -q_1 \cdot (x_3)^2/2 + R_A \cdot (x_3 - 3) + R_B \cdot (x_3 - 11.1666)$$

The values of M at the edges of the span:

$$M_3(11.17) = -4753 \cdot (11.17 - 0)^2/2 + 33666.92 \cdot (11.17 - 3) + 33666.92 \cdot (11.17 - 11.1666) = -21388.50 \text{ (lbf*ft)}$$

$$M_3(14.17) = -4753 \cdot (14.17 - 0)^2/2 + 33666.92 \cdot (14.17 - 3) + 33666.92 \cdot (14.17 - 11.1666) = 0 \text{ (lbf*ft)}$$

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